Outline

Distributional Semantic Models

Part 2: The parameters of a DSM

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http://wordspace.collocations.de/doku.php/course:start

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DSM parameters

General definition of DSMs

A distributional semantic model (DSM) is a scaled and/or transformed co-occurrence matrix \mathbf{M} , such that each row \mathbf{x} represents the distribution of a target term across contexts.

| | get | see | use | hear | eat | kill |
|--------|--------|--------|--------|--------|--------|--------|
| knife | 0.027 | -0.024 | 0.206 | -0.022 | -0.044 | -0.042 |
| cat | 0.031 | 0.143 | -0.243 | -0.015 | -0.009 | 0.131 |
| dog | -0.026 | 0.021 | -0.212 | 0.064 | 0.013 | 0.014 |
| boat | -0.022 | 0.009 | -0.044 | -0.040 | -0.074 | -0.042 |
| cup | -0.014 | -0.173 | -0.249 | -0.099 | -0.119 | -0.042 |
| pig | -0.069 | 0.094 | -0.158 | 0.000 | 0.094 | 0.265 |
| banana | 0.047 | -0.139 | -0.104 | -0.022 | 0.267 | -0.042 |

Term = word, lemma, phrase, morpheme, word pair, ...

Outline

DSM parameters

A taxonomy of DSM parameters Examples

Building a DSM

Sparse matrices Example: a verb-object DSM

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DSM parameters

General definition of DSMs

Mathematical notation:

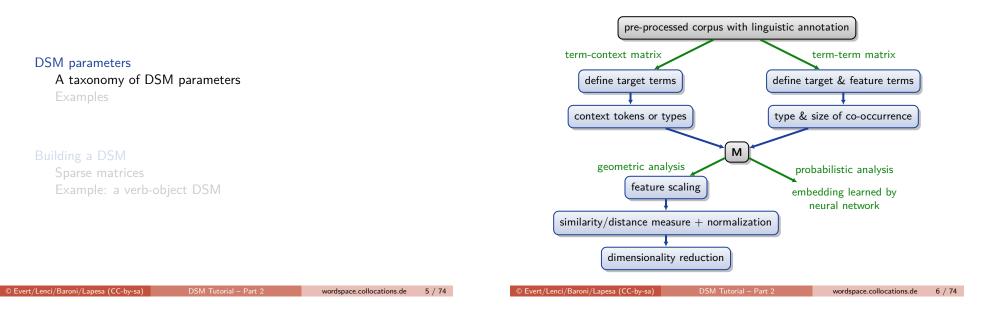
- $k \times n$ co-occurrence matrix $\mathbf{M} \in \mathbb{R}^{k \times n}$ (example: 7 × 6)
 - ► *k* rows = **target** terms
 - n columns = features or dimensions
 - $\mathbf{M} = \begin{bmatrix} m_{11} & m_{12} & \cdots & m_{1n} \\ m_{21} & m_{22} & \cdots & m_{2n} \\ \vdots & \vdots & & \vdots \\ m_{k1} & m_{k2} & \cdots & m_{kn} \end{bmatrix}$
- ▶ distribution vector $\mathbf{m}_i = i$ -th row of \mathbf{M} , e.g. $\mathbf{m}_3 = \mathbf{m}_{dog} \in \mathbb{R}^n$
- components $\mathbf{m}_i = (m_{i1}, m_{i2}, \dots, m_{in})$ = features of *i*-th term:

 $\mathbf{m}_3 = (-0.026, 0.021, -0.212, 0.064, 0.013, 0.014)$

 $=(m_{31}, m_{32}, m_{33}, m_{34}, m_{35}, m_{36})$

Outline

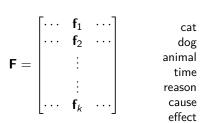
Overview of DSM parameters



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Term-context matrix

Term-context matrix records frequency of term in each individual context (e.g. sentence, document, Web page, encyclopaedia article)



| | c | 7, | | | | Ja. | - | ali, |
|--------|---------|----------------------|-------|-------|--------|----------|--|------|
| | Felidas | ې 2 ⁶⁰ | Feral | Bloat | Philos | - Kant - | en de la | ~ |
| cat | 10 | 10 | 7 | - | - | - | - | |
| dog | - | 10 | 4 | 11 | Ι | - | - | |
| animal | 2 | 15 | 10 | 2 | - | - | - | |
| time | 1 | - | - | - | 2 | 1 | - | |
| reason | - | 1 | - | - | 1 | 4 | 1 | |
| cause | - | - | - | 2 | 1 | 2 | 6 | |
| effect | - | - | - | 1 | - | 1 | - | |
| | | | | | | | | |

> TC <- DSM_TermContext

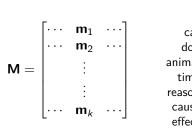
> head(TC, Inf) # extract full co-oc matrix from DSM object

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Term-term matrix

Term-term matrix records co-occurrence frequencies with feature terms for each target term

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| | δ | , | | | | | £ ,3 |
|--------|-------|------|------|------|----|--------|--------|
| | breed | ťaji | reed | kill | im | etols. | likel, |
| cat | 83 | 17 | 7 | 37 | - | 1 | - |
| dog | 561 | 13 | 30 | 60 | 1 | 2 | 4 |
| animal | 42 | 10 | 109 | 134 | 13 | 5 | 5 |
| time | 19 | 9 | 29 | 117 | 81 | 34 | 109 |
| reason | 1 | - | 2 | 14 | 68 | 140 | 47 |
| cause | - | 1 | - | 4 | 55 | 34 | 55 |
| effect | - | - | 1 | 6 | 60 | 35 | 17 |

> TT <- DSM_TermTerm
> head(TT, Inf)

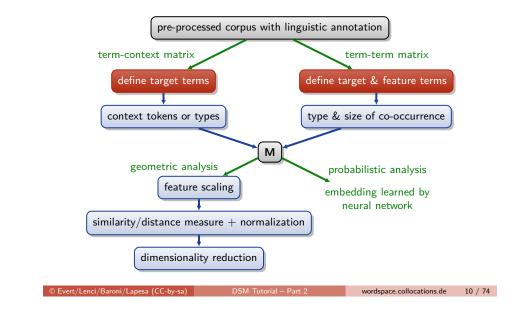
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Term-term matrix

Some footnotes:

- Often target terms \neq feature terms
 - e.g. nouns described by co-occurrences with verbs as features
 - ▶ identical sets of target & feature terms → symmetric matrix
- Different types of co-occurrence (Evert 2008)
 - surface context (word or character window)
 - textual context (non-overlapping segments)
 - syntactic context (dependency relation)
- Can be seen as smoothing of term-context matrix
 - average over similar contexts (with same context terms)
 - data sparseness reduced, except for small windows
 - we will take a closer look at the relation between term-context and term-term models in part 5 of this tutorial

Overview of DSM parameters



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Definition of target and feature terms

- Choice of linguistic unit
 - words

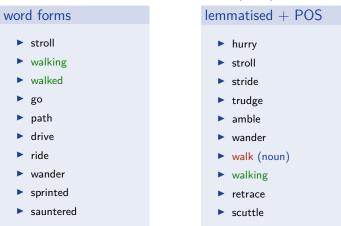
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- bigrams, trigrams,
- multiword units, named entities, phrases,
- morphemes
- word pairs (10% analogy tasks)
- Linguistic annotation
 - word forms (minimally requires tokenisation)
 - often lemmatisation or stemming to reduce data sparseness: go, goes, went, gone, going → go
 - POS disambiguation (*light*/N vs. *light*/A vs. *light*/V)
 - word sense disambiguation (bankriver vs. bankfinance)
 - abstraction: POS tags (or bigrams) as feature terms
- Trade-off between deeper linguistic analysis and
 - need for language-specific resources
 - possible errors introduced at each stage of the analysis

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Effects of linguistic annotation

Nearest neighbours of *walk* (BNC)



http://clic.cimec.unitn.it/infomap-query/

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► go

path

ride

Effects of linguistic annotation

Nearest neighbours of arrivare (Repubblica)

| word forms | lemmatised + POS |
|--------------------------------|--|
| giungere | ► giungere |
| raggiungere | ► aspettare |
| arrivi | attendere |
| raggiungimento | arrivo (noun) |
| raggiunto | ricevere |
| trovare | accontentare |
| raggiunge | approdare |
| arrivasse | pervenire |
| arriverà | venire |
| concludere | piombare |
| | http://clic.cimec.unitn.it/infomap-query/ |
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Selection of target and feature terms

 Full-vocabulary models are often unmanageable 762.424 distinct word forms in BNC. 605.910 lemmata large Web corpora have > 10 million distinct word forms Iow-frequency targets (and features) do not provide reliable distributional information (too much "noise") Frequency-based selection • minimum corpus frequency: $f > F_{min}$ • or accept n_w most frequent terms • sometimes also upper threshold: $F_{\min} \leq f \leq F_{\max}$ Relevance-based selection criterion from IR: document frequency df • terms with high df are too general \rightarrow uninformative terms with very low df may be too sparse to be useful Other criteria POS-based filter: no function words, only verbs, © Evert/Lenci/Baroni/Lapesa (CC-by-sa) wordspace.collocations.de

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Surface context

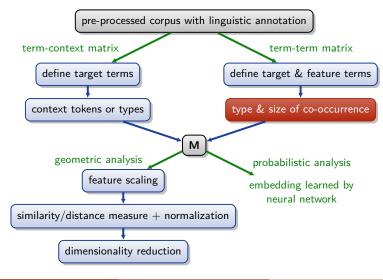
Context term occurs within a span of k words around target.

The silhouette of the sun beyond a wide-open bay on the lake; the sun still glitters although evening has arrived in Kuhmo. It's midsummer; the living room has its instruments and other objects in each of its corners. [L3/R3 span, k = 6]

Parameters:

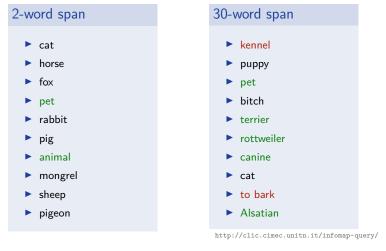
- span size (in words or characters)
- symmetric vs. one-sided span
- uniform or "triangular" (distance-based) weighting
- spans clamped to sentences or other textual units?

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Effect of span size

Nearest neighbours of *dog* (BNC)



Textual context

Context term is in the same linguistic unit as target.

The silhouette of the sun beyond a wide-open bay on the lake; the sun still glitters although evening has arrived in Kuhmo. It's midsummer; the living room has its instruments and other objects in each of its corners.

Parameters:

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- type of linguistic unit
 - sentence
 - paragraph
 - turn in a conversation
 - Web page

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Syntactic context

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Context term is linked to target by a syntactic dependency (e.g. subject, modifier, ...).

The silhouette of the sun beyond a wide-open bay on the lake; the sun still glitters although evening has arrived in Kuhmo. It's midsummer; the living room has its instruments and other objects in each of its corners.

Parameters:

- types of syntactic dependency (Padó and Lapata 2007)
- direct vs. indirect dependency paths
 - direct dependencies
 - direct + indirect dependencies
- homogeneous data (e.g. only verb-object) vs. heterogeneous data (e.g. all children and parents of the verb)
- maximal length of dependency path

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"Knowledge pattern" context

Context term is linked to target by a lexico-syntactic pattern (text mining, cf. Hearst 1992, Pantel & Pennacchiotti 2008, etc.).

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In Provence, Van Gogh painted with bright colors such as red and yellow. These colors produce incredible effects on anybody looking at his paintings.

Parameters:

- inventory of lexical patterns
 - Iots of research to identify semantically interesting patterns (cf. Almuhareb & Poesio 2004, Veale & Hao 2008, etc.)
- ► fixed vs. flexible patterns
 - patterns are mined from large corpora and automatically generalised (optional elements, POS tags or semantic classes)

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In unstructered models, context specification acts as a filter
 determines whether context token counts as co-occurrence
 e.g. muste be linked by any syntactic dependency relation

• e.g. left vs. right context, type of syntactic relation, etc.

In structured models, feature terms are subtyped

depending on their position in the context

Structured vs. unstructured context

Structured vs. unstructured surface context

A dog bites a man. The man's dog bites a dog. A dog bites a man.

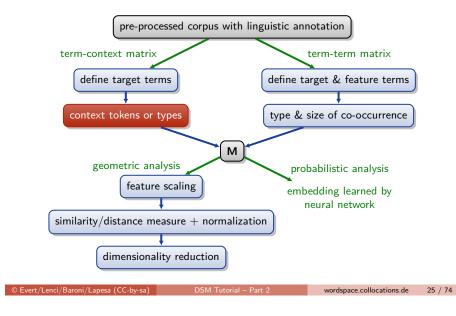
| unstructured | bite |
|--------------|------|
| dog | 4 |
| man | 3 |

A dog bites a man. The man's dog bites a dog. A dog bites a man.

| structured | bite-l | bite-r |
|------------|--------|--------|
| dog | 3 | 1 |
| man | 1 | 2 |

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|--|-------------|--|--|---|---------|--|--|
| DSM parameters A taxonomy of DSM parameters | | | DSM parameters A taxonomy of D | DSM parameters | | | |
| Structured vs. unstructured dependency context | | Comparison | | | | | |
| A dog bites a man. The man's dog bites a dog. A dog bites a n unstructured bite dog 4 man 2 | nan. | Unstructured context data less sparse (e.g. man kills and kills man both map to the kill dimension of the vector x_{man}) Structured context | | | | | |
| A dog bites a man. The man's dog bites a dog. A dog bites a n structured bite-subj bite-obj dog 3 1 man 0 2 | nan. | (<i>kill-subj</i> and <i>i</i> ► dependency re the DSM dime "recipient" dim | to semantic distinctions kill-obj are rather differen lations provide a form of ensions (the "subject" di nensions, etc.) account for word-order an | nt things!) f syntactic "typing" of mensions, the | | | |

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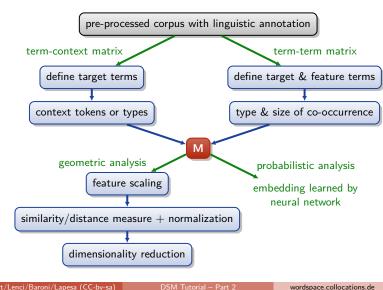


Context tokens vs. context types

- ▶ Features are usually context tokens, i.e. individual instances
 - document, Wikipedia article, Web page, ...
 - paragraph, sentence, tweet,
 - "co-occurrence" count = frequency of term in context token
- Can also be generalised to context types, e.g.
 - type = cluster of near-duplicate documents
 - type = syntactic structure of sentence (ignoring content)
 - type = tweets from same author
 - frequency counts from all instances of type are aggregated
- Context types may be anchored at individual tokens
 - n-gram of words (or POS tags) around target
 - subcategorisation pattern of target verb
 - overlaps with (generalisation of) syntactic co-occurrence

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Marginal and expected frequencies

Matrix of observed co-occurrence frequencies not sufficient

| target | feature | 0 | R | С | Е |
|--------|--------------|-----|--------|---------|--------|
| dog | small | 855 | 33,338 | 490,580 | 134.34 |
| dog | domesticated | 29 | 33,338 | 918 | 0.25 |

Notation

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- O =observed co-occurrence frequency
- \triangleright R = overall frequency of target term = row marginal frequency
- C =overall frequency of feature = column marginal frequency
- N = sample size \approx size of corpus
- Expected co-occurrence frequency

$$E = \frac{R \cdot C}{N} \quad \longleftrightarrow \quad O$$

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Obtaining marginal frequencies

- Term-document matrix
 - \blacktriangleright R = frequency of target term in corpus
 - C = size of document (# tokens)
 - ► *N* = corpus size
- Syntactic co-occurrence
 - # of dependency instances in which target/feature participates
 - ► *N* = total number of dependency instances
 - ► can be computed from full co-occurrence matrix M
- Textual co-occurrence

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- R, C, O are "document" frequencies, i.e. number of context units in which target, feature or combination occurs
- N = total # of context units

Obtaining marginal frequencies

- Surface co-occurrence
 - it is quite tricky to obtain fully consistent counts (Evert 2008)
 - at least correct E for span size k (= number of tokens in span)

$$E = k \cdot \frac{R \cdot C}{N}$$

with R, C = individual corpus frequencies and N = corpus size

- can also be implemented by pre-multiplying $R' = k \cdot R$
- alternatively, compute marginals and sample size by summing over full co-occurrence matrix ($\rightarrow E$ as above, but inflated N)
- NB: shifted PPMI (Levy and Goldberg 2014) corresponds to a post-hoc application of the span size adjustment
 - performs worse than PPMI, but paper suggests they already approximate correct *E* by summing over co-occurrence matrix

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Marginal frequencies in wordspace

DSM objects in wordspace include marginal frequencies as well as counts of nonzero cells for rows and columns.

| > | TT\$row | S | |
|----|---------|------------|---------|
| | term | f | nnzero |
| 1 | cat | 22007 | 5 |
| 2 | dog | 50807 | 7 |
| 3 | animal | 77053 | 7 |
| 4 | time | 1156693 | 7 |
| 5 | reason | 95047 | 6 |
| 6 | cause | 54739 | 5 |
| 7 | effect | 133102 | 6 |
| > | TT\$col | S | |
| | | | |
| > | TT\$glo | bals\$N | |
| [1 |] 19990 | 2178 | |
| > | TT\$M # | ≠ the full | ςο-οςςι |
| 1 | 11ψΠ 7 | - the full | |

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Geometric vs. probabilistic interpretation

► Geometric interpretation

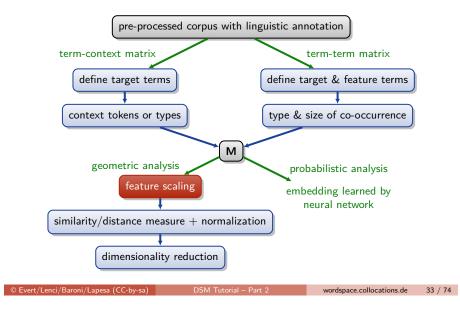
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- row vectors as points or arrows in *n*-dimensional space
- very intuitive, good for visualisation
- use techniques from geometry and matrix algebra
- Probabilistic interpretation
 - co-occurrence matrix as observed sample statistic that is "explained" by a generative probabilistic model
 - e.g. probabilistic LSA (Hoffmann 1999), Latent Semantic Clustering (Rooth *et al.* 1999), Latent Dirichlet Allocation (Blei *et al.* 2003), etc.
 - explicitly accounts for random variation of frequency counts
 - recent work: neural word embeddings

so focus on geometric interpretation in this tutorial

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Feature scaling

Feature scaling is used to "discount" less important features:

- Logarithmic scaling: O' = log(O + 1) (cf. Weber-Fechner law for human perception)
- Relevance weighting, e.g. tf.idf (information retrieval)

$$tf.idf = tf \cdot log(D/df)$$

- ► *tf* = co-occurrence frequency *O*
- df = document frequency of feature (or nonzero count)
- ► *D* = total number of documents (or row count of **M**)
- Statistical association measures (Evert 2004, 2008) take frequency of target term and feature into account
 - often based on comparison of observed and expected co-occurrence frequency

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measures differ in how they balance O and E

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Simple association measures

pointwise Mutual Information (MI)

$$\mathsf{MI} = \log_2 \frac{O}{E}$$

local MI

$$|\text{local-MI} = O \cdot \text{MI} = O \cdot \log_2 \frac{O}{E}$$

t-score

 $t = \frac{O - E}{\sqrt{O}}$

| target | feature | 0 | Ε | MI | local-MI | t-score |
|--------|--------------|-----|---------|-------|----------|---------|
| dog | small | 855 | 134.34 | 2.67 | 2282.88 | 24.64 |
| dog | domesticated | 29 | 0.25 | 6.85 | 198.76 | 5.34 |
| dog | sgjkj | 1 | 0.00027 | 11.85 | 11.85 | 1.00 |

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Other association measures

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• simple log-likelihood (\approx local-MI)

$$G^2 = \pm 2 \cdot \left(O \cdot \log_2 \frac{O}{E} - (O - E) \right)$$

with positive sign for O > E and negative sign for O < E

Dice coefficient

$$\mathsf{Dice} = \frac{20}{R+6}$$

~ ~

- Many other simple association measures (AMs) available
- ▶ Further AMs computed from full contingency tables, see
 - Evert (2008)
 - http://www.collocations.de/
 - http://sigil.r-forge.r-project.org/

Applying association scores in wordspace

| <pre>> options(digits=3)</pre> | # print fractional values with limited precision |
|-----------------------------------|--|
| > dsm.score(TT. scor | e="MI", sparse=FALSE, matrix=TRUE) |

| | breed | tail | feed | kill | important | explain | likely |
|--------|-------|--------|--------|--------|-----------|---------|---------|
| cat | 6.21 | 4.568 | 3.129 | 2.801 | -Inf | 0.0182 | -Inf |
| dog | 7.78 | 3.081 | 3.922 | 2.323 | -3.774 | -1.1888 | -0.4958 |
| animal | 3.50 | 2.132 | 4.747 | 2.832 | -0.674 | -0.4677 | -0.0966 |
| time | -1.65 | -2.236 | -0.729 | -1.097 | -1.728 | -1.2382 | 0.6392 |
| reason | -2.30 | -Inf | -1.982 | -0.388 | 1.472 | 4.0368 | 2.8860 |
| cause | -Inf | -0.834 | -Inf | -2.177 | 1.900 | 2.8329 | 4.0691 |
| effect | -Inf | -2.116 | -2.468 | -2.459 | 0.791 | 1.6312 | 0.9221 |

- ☞ sparseness of the matrix has been lost!
- \bowtie cells with score $x = -\infty$ are inconvenient
- distribution of scores may be even more skewed than co-occurrence frequencies (esp. for local-MI)

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Sparse association scores are cut off at zero, i.e.

$$f(x) = \begin{cases} x & x > 0 \\ 0 & x \le 0 \end{cases}$$

- Also known as "positive" scores
 - ▶ PPMI = positive pointwise MI (e.g. Bullinaria and Levy 2007)
 - wordspace computes sparse AMs by default \rightarrow "MI" = PPMI
- Preserves sparseness if $x \le 0$ for all empty cells (O = 0)
 - sparseness may even increase: cells with x < 0 become empty
- Usually combined with signed association measure satisfying

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- ► x > 0 for O > E
- x < 0 for O < E

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Score transformations

An additional scale transformation can be applied in order to de-skew association scores:

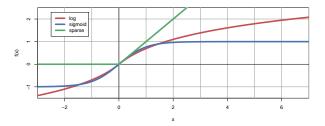
signed logarithmic transformation

$$f(x) = \pm \log(|x|+1)$$

sigmoid transformation as soft binarization

$$f(x) = \tanh x$$

sparse AM as cutoff transformation



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Association scores & transformations in wordspace

| <pre>> dsm.score(TT, score="simple-ll", transf="lo # logarithmic co-occurrence frequency</pre> | у | | | | | | | |
|--|--|--|--|--|--|--|--|--|
| animal 3.50 2.13 4.75 2.83 0.000 0.0000 0.0 time 0.00 0.00 0.00 0.00 0.000 0.000 0.000 reason 0.00 0.00 0.00 0.00 1.472 4.0368 2.8 cause 0.00 0.00 0.00 0.00 1.900 2.8329 4.0 effect 0.00 0.00 0.00 0.00 0.791 1.6312 0.9 > dsm.score(TT, score="simple-ll", matrix=TRU > dsm.score(TT, score="simple-ll", transf="lo # logarithmic co-occurrence frequency | 0 | | | | | | | |
| <pre>time 0.00 0.00 0.00 0.00 0.000 0.000 0.6 reason 0.00 0.00 0.00 0.00 1.472 4.0368 2.8 cause 0.00 0.00 0.00 0.00 1.900 2.8329 4.0 effect 0.00 0.00 0.00 0.00 0.791 1.6312 0.9 > dsm.score(TT, score="simple-ll", matrix=TRU > dsm.score(TT, score="simple-ll", transf="lo # logarithmic co-occurrence frequency</pre> | 0 | | | | | | | |
| <pre>reason 0.00 0.00 0.00 0.00 1.472 4.0368 2.8 cause 0.00 0.00 0.00 0.00 1.900 2.8329 4.0 effect 0.00 0.00 0.00 0.00 0.791 1.6312 0.9 > dsm.score(TT, score="simple-ll", matrix=TRU > dsm.score(TT, score="simple-ll", transf="lo # logarithmic co-occurrence frequency</pre> | 0 | | | | | | | |
| <pre>cause 0.00 0.00 0.00 0.00 1.900 2.8329 4.0 effect 0.00 0.00 0.00 0.00 0.791 1.6312 0.9 > dsm.score(TT, score="simple-ll", matrix=TRU > dsm.score(TT, score="simple-ll", transf="lo # logarithmic co-occurrence frequency</pre> | 9 | | | | | | | |
| <pre>effect 0.00 0.00 0.00 0.00 0.791 1.6312 0.9 > dsm.score(TT, score="simple-ll", matrix=TRU > dsm.score(TT, score="simple-ll", transf="lo # logarithmic co-occurrence frequency</pre> | 6 | | | | | | | |
| <pre>> dsm.score(TT, score="simple-ll", matrix=TRU > dsm.score(TT, score="simple-ll", transf="lo # logarithmic co-occurrence frequency</pre> | 9 | | | | | | | |
| <pre>> dsm.score(TT, score="simple-ll", transf="lo # logarithmic co-occurrence frequency</pre> | 2 | | | | | | | |
| # logarithmic co-occurrence frequency | <pre>> dsm.score(TT, score="simple-ll", matrix=TRUE)</pre> | | | | | | | |
| | <pre>> dsm.score(TT, score="simple-ll", transf="log", matrix=T)</pre> | | | | | | | |
| <pre>> dsm.score(TT, score="freq", transform="log"</pre> | # logarithmic co-occurrence frequency | | | | | | | |
| | <pre>> dsm.score(TT, score="freq", transform="log", matrix=T)</pre> | | | | | | | |
| | | | | | | | | |
| # now try other parameter combinations | | | | | | | | |

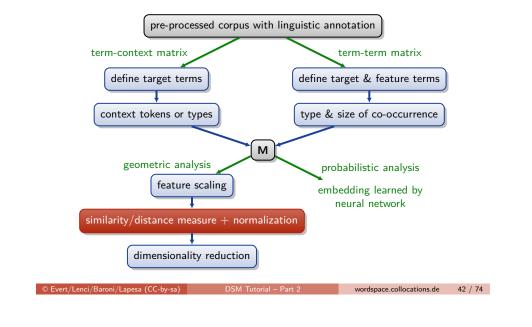
Scaling of column vectors

In statistical analysis and machine learning, features are usually centred and scaled so that

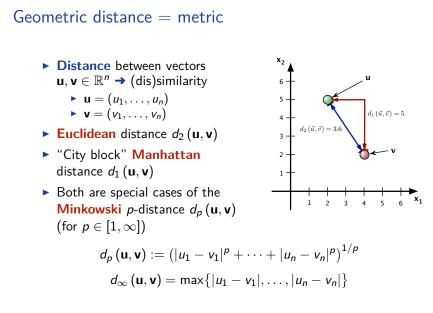
$$\begin{array}{ll} {\rm mean} & \mu = {\rm 0} \\ {\rm variance} & \sigma^2 = {\rm 1} \end{array}$$

- ► In DSM research, this step is less common for columns of M
 - centring is a prerequisite for certain dimensionality reduction and data analysis techniques (esp. PCA)
 - but co-occurrence matrix no longer sparse!
 - scaling may give too much weight to rare features
- M cannot be row-normalised and column-scaled at the same time (result depends on ordering of the two steps)

Overview of DSM parameters



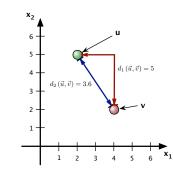
DSM parameters A taxonomy of DSM parameters

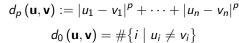


DSM parameters A taxonomy of DSM parameters Geometric distance = metric

$$\mathbf{u}, \mathbf{v} \in \mathbb{R}^n \Rightarrow (dis)$$
similarity

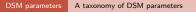
- $\bullet \mathbf{u} = (u_1, \dots, u_n)$ $\bullet \mathbf{v} = (v_1, \dots, v_n)$
- Euclidean distance $d_2(\mathbf{u}, \mathbf{v})$
- "City block" Manhattan distance d₁ (u, v)
- Extension of *p*-distance $d_p(\mathbf{u}, \mathbf{v})$ (for $0 \le p \le 1$)



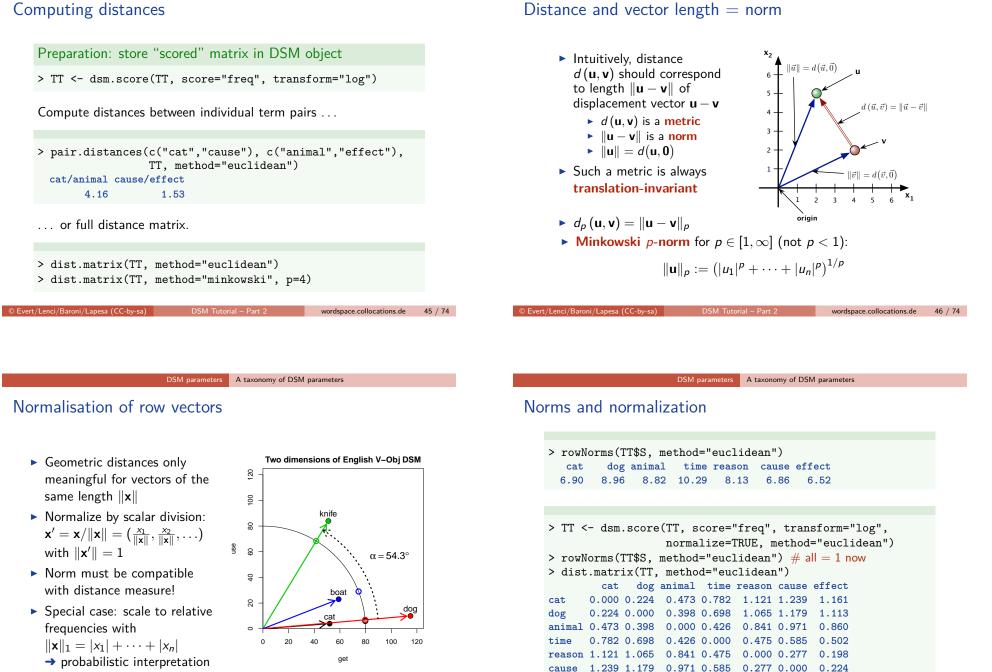


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Computing distances



effect 1.161 1.113 0.860 0.502 0.198 0.224 0.000

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Other distance measures

Information theory: Kullback-Leibler (KL) divergence for probability vectors (☞ non-negative, ||x||₁ = 1)

$$D(\mathbf{u} \| \mathbf{v}) = \sum_{i=1}^{n} u_i \cdot \log_2 \frac{u_i}{v_i}$$

- Properties of KL divergence
 - most appropriate in a probabilistic interpretation of M
 - \blacktriangleright zeroes in ${\bf v}$ without corresponding zeroes in ${\bf u}$ are problematic
 - not symmetric, unlike geometric distance measures
 - ▶ alternatives: skew divergence, Jensen-Shannon divergence
- A symmetric distance measure (Endres and Schindelin 2003)

$$D_{uv} = D(u||z) + D(v||z)$$
 with $z = \frac{u+v}{2}$

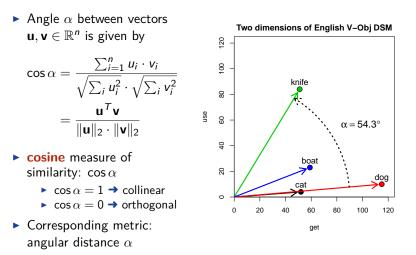
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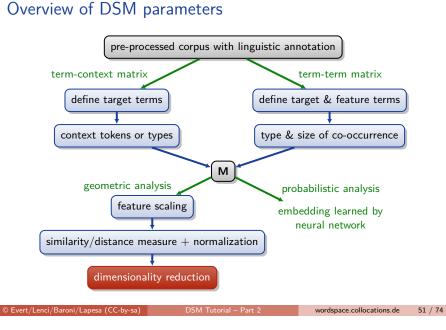
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DSM parameters A taxonomy of DSM parameters

DSM parameters A taxonomy of DSM parameters



Dimensionality reduction = model compression

- Co-occurrence matrix M is often unmanageably large and can be extremely sparse
 - Google Web1T5: 1M × 1M matrix with one trillion cells, of which less than 0.05% contain nonzero counts (Evert 2010)
- Compress matrix by reducing dimensionality (= rows)
- **Feature selection**: columns with high frequency & variance
 - measured by entropy, chi-squared test, nonzero count, ...
 - may select similar dimensions and discard valuable information
 - joint selection of multiple features is useful but expensive
- Projection into (linear) subspace
 - principal component analysis (PCA)
 - independent component analysis (ICA)
 - random indexing (RI)

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intuition: preserve distances between data points

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Dimensionality reduction & latent dimensions

Landauer and Dumais (1997) claim that LSA dimensionality reduction (and related PCA technique) uncovers **latent dimensions** by exploiting correlations between features.

- Example: term-term matrix
- V-Obj cooc's extracted from BNC
 - targets = noun lemmas
 - features = verb lemmas
- feature scaling: association scores (modified log Dice coefficient)
- k = 111 nouns with f ≥ 20 (must have non-zero row vectors)
- n = 2 dimensions: *buy* and *sell*

```
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```

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buv

0.28

-0.52

0.51

-0.01

1.13

-1.05

-0.35

-0.08

1.92

-1.63

noun

bond

dress

land

per

pub

share

system

cigarette

freehold

number

sell

0.77

0.44

-1.30

-0.08

1.54

-1.02

-0.16

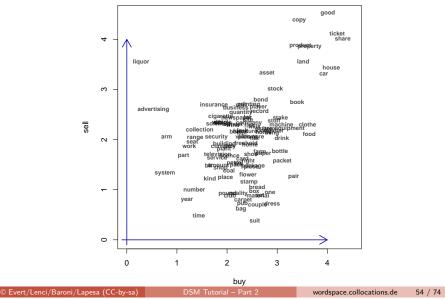
-1.30

1.99

-0.70

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Dimensionality reduction & latent dimensions



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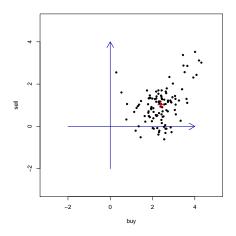
Motivating latent dimensions & subspace projection

- The latent property of being a commodity is "expressed" through associations with several verbs: sell, buy, acquire, ...
- Consequence: these DSM dimensions will be correlated
- Identify latent dimension by looking for strong correlations (or weaker correlations between large sets of features)
- Projection into subspace V of k < n latent dimensions as a "noise reduction" technique → LSA
- Assumptions of this approach:
 - "latent" distances in V are semantically meaningful
 - other "residual" dimensions represent chance co-occurrence patterns, often particular to the corpus underlying the DSM

DSM parameters A taxonomy of DSM parameters

Centering the data set

- Uncentered data set
- Centered data set
- Variance of centered data



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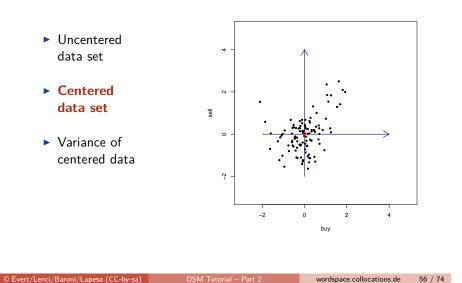
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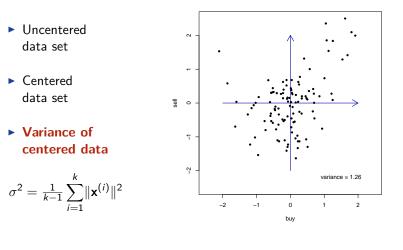
Centering the data set

Centering the data set

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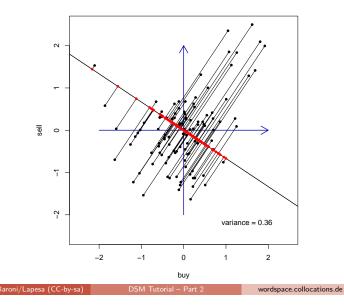
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DSM parameters A taxonomy of DSM parameters

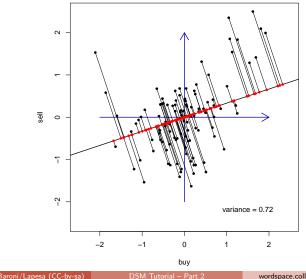
Projection and preserved variance: examples



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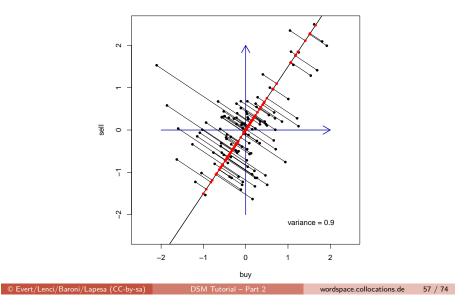
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Projection and preserved variance: examples

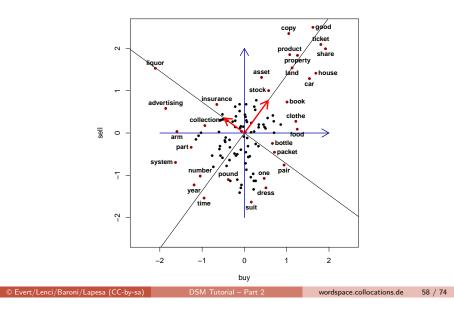


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Projection and preserved variance: examples



Orthogonal PCA dimensions



DSM parameters Examples

DSM parameters A taxonomy of DSM parameters

Dimensionality reduction in practice

```
\# it is customary to omit the centring: SVD dimensionality reduction
> TT2 <- dsm.projection(TT, n=2, method="svd")</pre>
> TT2
                svd2
         svd1
       -0.733 -0.6615
cat
       -0.782 -0.6110
dog
animal -0.914 -0.3606
       -0.993 0.0302
time
reason -0.889 0.4339
cause -0.817 0.5615
effect -0.871 0.4794
> x <- TT2[, 1] # first latent dimension
> y <- TT2[, 2] # second latent dimension
> plot(TT2, pch=20, col="red",
        xlim=extendrange(x), ylim=extendrange(y))
> text(TT2, rownames(TT2), pos=3)
```

Outline

DSM parameters

A taxonomy of DSM parameters Examples

Example: a verb-object DSM

Some well-known DSM examples

Latent Semantic Analysis (Landauer and Dumais 1997)

- term-context matrix with document context
- weighting: log term frequency and term entropy
- distance measure: cosine
- dimensionality reduction: SVD

Hyperspace Analogue to Language (Lund and Burgess 1996)

- term-term matrix with surface context
- structured (left/right) and distance-weighted frequency counts
- distance measure: Minkowski metric $(1 \le p \le 2)$
- dimensionality reduction: feature selection (high variance)

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DSM parameters Examples

Some well-known DSM examples

Infomap NLP (Widdows 2004)

- term-term matrix with unstructured surface context
- weighting: none
- distance measure: cosine
- dimensionality reduction: SVD

Random Indexing (Karlgren and Sahlgren 2001)

- term-term matrix with unstructured surface context
- weighting: various methods
- distance measure: various methods
- dimensionality reduction: random indexing (RI)

DSM parameters Examples

Some well-known DSM examples

Dependency Vectors (Padó and Lapata 2007)

- term-term matrix with unstructured dependency context
- weighting: log-likelihood ratio
- distance measure: PPMI-weighted Dice (Lin 1998)
- dimensionality reduction: none

Distributional Memory (Baroni and Lenci 2010)

- term-term matrix with structured and unstructered dependencies + knowledge patterns
- weighting: local-MI on type frequencies of link patterns
- distance measure: cosine
- dimensionality reduction: none

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Building a DSM Sparse matrices

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Building a DSM

Sparse matrices Example: a verb-object DSM

Building a DSM Sparse matrices

Building a DSM Sparse matrices

Scaling up to the real world

- ► So far, we have worked on minuscule toy models
- We want to scale up to real world data sets now
- ► Example 1: window-based DSM on BNC content words
 - ▶ 83,926 lemma types with $f \ge 10$
 - term-term matrix with $83,926 \cdot 83,926 = 7$ billion entries
 - standard representation requires 56 GB of RAM (8-byte floats)
 - only 22.1 million non-zero entries (= 0.32%)
- Example 2: Google Web 1T 5-grams (1 trillion words)
 - more than 1 million word types with $f \ge 2500$
 - term-term matrix with 1 trillion entries requires 8 TB RAM

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• only 400 million non-zero entries (= 0.04%)

| <u> </u> | 1 State 1 Stat | |
|----------|--|----------------|
| Snarco | matrix | representation |
| Juaise | IIIalin | TEDIESCITALION |
| | | |

Invented example of a sparsely populated DSM matrix

| _ | eat | get | hear | kill | see | use |
|-------|-----|-----|------|------|-----|-----|
| boat | . | 59 | • | • | 39 | 23 |
| cat | . | • | • | 26 | 58 | • |
| cup | . | 98 | • | • | • | • |
| dog | 33 | • | 42 | • | 83 | • |
| knife | . | • | • | • | • | 84 |
| pig | 9 | • | • | 27 | • | • |

Store only non-zero entries in compact sparse matrix format

| row | col | value | r | wo | col | value |
|-----|-----|-------|---|----|-----|-------|
| 1 | 2 | 59 | | 4 | 1 | 33 |
| 1 | 5 | 39 | | 4 | 3 | 42 |
| 1 | 6 | 23 | | 4 | 5 | 83 |
| 2 | 4 | 26 | | 5 | 6 | 84 |
| 2 | 5 | 58 | | 6 | 1 | 9 |
| 3 | 2 | 98 | | 6 | 4 | 27 |

Building a DSM Example: a verb-object DSM

Building a DSM Sparse matrices

Working with sparse matrices

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- Compressed format: each row index (or column index) stored only once, followed by non-zero entries in this row (or column)
 - convention: column-major matrix (data stored by columns)
- Specialised algorithms for sparse matrix algebra
 - especially matrix multiplication, solving linear systems, etc.
 - take care to avoid operations that create a dense matrix!
- R implementation: Matrix package
 - essential for real-life distributional semantics
 - wordspace provides additional support for sparse matrices (vector distances, sparse SVD, ...)
- Other software: Matlab, Octave, Python + SciPy

Outline

DSM parameters

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Building a DSM

Sparse matrices Example: a verb-object DSM

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Triplet tables

- A sparse DSM matrix can be represented as a table of triplets (target, feature, co-occurrence frequency)
 - for syntactic co-occurrence and term-document matrices, marginals can be computed from a complete triplet table
 - > for surface and textual co-occurrence, marginals have to be provided in separate files (see ?read.dsm.triplet)

| noun | rel | verb | f | mode |
|------|------|--------|----|---------|
| dog | subj | bite | 3 | spoken |
| dog | subj | bite | 12 | written |
| dog | obj | bite | 4 | written |
| dog | obj | stroke | 3 | written |
| | | | | |

- DSM_VerbNounTriples_BNC contains additional information
 - syntactic relation between noun and verb
 - written or spoken part of the British National Corpus

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 Additional information can be used for filtering (verb-object relation), or aggregate frequencies (spoken + written BNC)

> tri <- subset(DSM_VerbNounTriples_BNC, rel == "obj")</pre>

Construct DSM object from triplet input

Constructing a DSM from a triplet table

- raw.freq=TRUE indicates raw co-occurrence frequencies (rather than a pre-weighted DSM)
- constructor aggregates counts from duplicate entries
- marginal frequencies are automatically computed
- > VObj # inspect marginal frequencies (e.g. head(VObj\$rows, 20))

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Building a DSM Example: a verb-object DSM

Exploring the DSM

| > VObj <- | dsm.sco | re(VObj, | score="N | II", norm | alize=TRUE |) |
|------------|----------|----------|-----------|-----------|------------|---|
| > nearest | 0 | 5 | . 0 | | | |
| horse | cat | animal | rabbit | fish | guy | |
| 73.9 | 75.9 | 76.2 | 77.0 | 77.2 | 78.5 | |
| cichlid | kid | bee c | reature | | | |
| 78.6 | 79.0 | 79.1 | 79.5 | | | |
| | | | | | | |
| > nearest | .neighbo | urs(VObj | , "dog", | method=" | manhattan" |) |
| # NB: we u | 0 | 0 | | | | |
| ,, | | | | | | |
| > VObi50 | - dem n | rojectio | n(VObir | n=50 mot | hod="svd") | |
| - | - | | - | | nou- svu) | |
| > nearest | .neighbo | urs(VObj | 50, "dog' | ') | | |

uilding a DSM Example: a verb-object DSM

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Building a DSM Example: a verb-object DSM

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