Outline

Distributional Semantic Models

Part 2: The parameters of a DSM

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http://wordspace.collocations.de/doku.php/course:start

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DSM parameters

General definition of DSMs

A distributional semantic model (DSM) is a scaled and/or transformed co-occurrence matrix \mathbf{M} , such that each row \mathbf{x} represents the distribution of a target term across contexts.

	get	see	use	hear	eat	kill
knife	0.027	-0.024	0.206	-0.022	-0.044	-0.042
cat	0.031	0.143	-0.243	-0.015	-0.009	0.131
dog	-0.026	0.021	-0.212	0.064	0.013	0.014
boat	-0.022	0.009	-0.044	-0.040	-0.074	-0.042
cup	-0.014	-0.173	-0.249	-0.099	-0.119	-0.042
pig	-0.069	0.094	-0.158	0.000	0.094	0.265
banana	0.047	-0.139	-0.104	-0.022	0.267	-0.042

Term = word, lemma, phrase, morpheme, word pair, ...

Outline

DSM parameters

A taxonomy of DSM parameters Examples

Building a DSM

Sparse matrices Example: a verb-object DSM

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DSM parameters

General definition of DSMs

Mathematical notation:

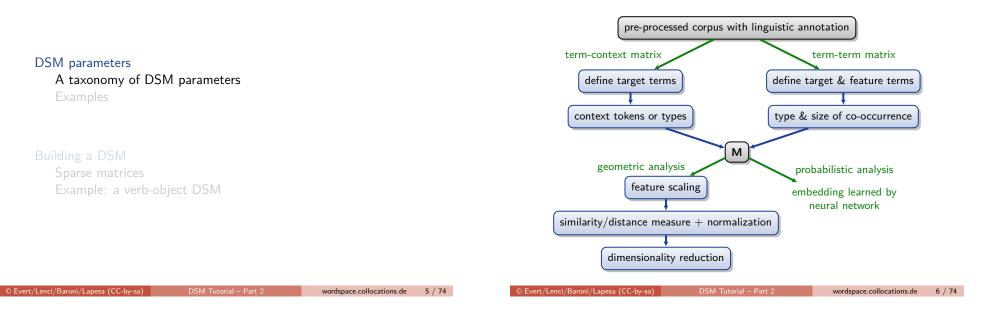
- $k \times n$ co-occurrence matrix $\mathbf{M} \in \mathbb{R}^{k \times n}$ (example: 7 × 6)
 - ► *k* rows = **target** terms
 - n columns = features or dimensions
 - $\mathbf{M} = \begin{bmatrix} m_{11} & m_{12} & \cdots & m_{1n} \\ m_{21} & m_{22} & \cdots & m_{2n} \\ \vdots & \vdots & & \vdots \\ m_{k1} & m_{k2} & \cdots & m_{kn} \end{bmatrix}$
- ▶ distribution vector $\mathbf{m}_i = i$ -th row of \mathbf{M} , e.g. $\mathbf{m}_3 = \mathbf{m}_{dog} \in \mathbb{R}^n$
- components $\mathbf{m}_i = (m_{i1}, m_{i2}, \dots, m_{in})$ = features of *i*-th term:

 $\mathbf{m}_3 = (-0.026, 0.021, -0.212, 0.064, 0.013, 0.014)$

 $=(m_{31}, m_{32}, m_{33}, m_{34}, m_{35}, m_{36})$

Outline

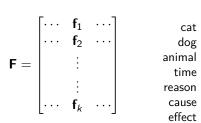
Overview of DSM parameters



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Term-context matrix

Term-context matrix records frequency of term in each individual context (e.g. sentence, document, Web page, encyclopaedia article)



	c	7,				Ja.	-	ali,
	Felidas	ې 2 ⁶⁰	Feral	Bloat	Philos	- Kant -	en de la	~
cat	10	10	7	-	-	-	-	
dog	-	10	4	11	Ι	-	-	
animal	2	15	10	2	-	-	-	
time	1	-	-	-	2	1	-	
reason	-	1	-	-	1	4	1	
cause	-	-	-	2	1	2	6	
effect	-	-	-	1	-	1	-	

> TC <- DSM_TermContext

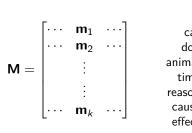
> head(TC, Inf) # extract full co-oc matrix from DSM object

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Term-term matrix

Term-term matrix records co-occurrence frequencies with feature terms for each target term

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	breed	ťaji	reed	kill	im	etols.	likel,
cat	83	17	7	37	-	1	-
dog	561	13	30	60	1	2	4
animal	42	10	109	134	13	5	5
time	19	9	29	117	81	34	109
reason	1	-	2	14	68	140	47
cause	-	1	-	4	55	34	55
effect	-	-	1	6	60	35	17

> TT <- DSM_TermTerm
> head(TT, Inf)

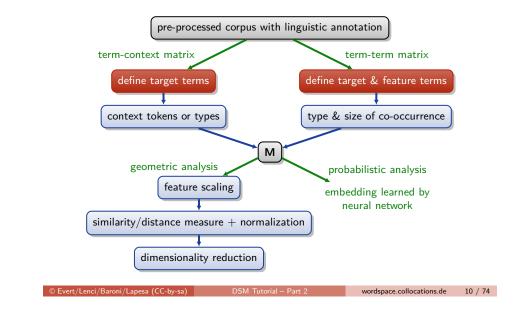
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Term-term matrix

Some footnotes:

- Often target terms \neq feature terms
 - e.g. nouns described by co-occurrences with verbs as features
 - ▶ identical sets of target & feature terms → symmetric matrix
- Different types of co-occurrence (Evert 2008)
 - surface context (word or character window)
 - textual context (non-overlapping segments)
 - syntactic context (dependency relation)
- Can be seen as smoothing of term-context matrix
 - average over similar contexts (with same context terms)
 - data sparseness reduced, except for small windows
 - we will take a closer look at the relation between term-context and term-term models in part 5 of this tutorial

Overview of DSM parameters



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Definition of target and feature terms

- Choice of linguistic unit
 - words

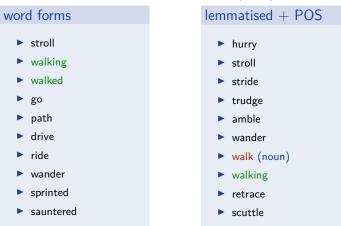
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- bigrams, trigrams,
- multiword units, named entities, phrases,
- morphemes
- word pairs (10% analogy tasks)
- Linguistic annotation
 - word forms (minimally requires tokenisation)
 - often lemmatisation or stemming to reduce data sparseness: go, goes, went, gone, going → go
 - POS disambiguation (*light*/N vs. *light*/A vs. *light*/V)
 - word sense disambiguation (bankriver vs. bankfinance)
 - abstraction: POS tags (or bigrams) as feature terms
- Trade-off between deeper linguistic analysis and
 - need for language-specific resources
 - possible errors introduced at each stage of the analysis

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Effects of linguistic annotation

Nearest neighbours of *walk* (BNC)



http://clic.cimec.unitn.it/infomap-query/

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► go

path

ride

Effects of linguistic annotation

Nearest neighbours of arrivare (Repubblica)

word forms	lemmatised + POS
 giungere 	► giungere
raggiungere	► aspettare
arrivi	attendere
raggiungimento	arrivo (noun)
raggiunto	ricevere
trovare	accontentare
 raggiunge 	approdare
arrivasse	pervenire
 arriverà 	venire
 concludere 	piombare
	http://clic.cimec.unitn.it/infomap-query/
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Selection of target and feature terms

 Full-vocabulary models are often unmanageable 762.424 distinct word forms in BNC. 605.910 lemmata large Web corpora have > 10 million distinct word forms Iow-frequency targets (and features) do not provide reliable distributional information (too much "noise") Frequency-based selection • minimum corpus frequency: $f > F_{min}$ • or accept n_w most frequent terms • sometimes also upper threshold: $F_{\min} \leq f \leq F_{\max}$ Relevance-based selection criterion from IR: document frequency df • terms with high df are too general \rightarrow uninformative terms with very low df may be too sparse to be useful Other criteria POS-based filter: no function words, only verbs, © Evert/Lenci/Baroni/Lapesa (CC-by-sa) wordspace.collocations.de

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Surface context

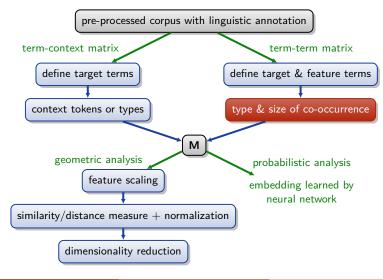
Context term occurs within a span of k words around target.

The silhouette of the sun beyond a wide-open bay on the lake; the sun still glitters although evening has arrived in Kuhmo. It's midsummer; the living room has its instruments and other objects in each of its corners. [L3/R3 span, k = 6]

Parameters:

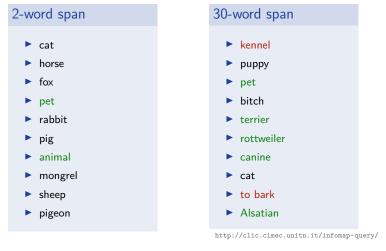
- span size (in words or characters)
- symmetric vs. one-sided span
- uniform or "triangular" (distance-based) weighting
- spans clamped to sentences or other textual units?

Overview of DSM parameters



Effect of span size

Nearest neighbours of *dog* (BNC)



Textual context

Context term is in the same linguistic unit as target.

The silhouette of the sun beyond a wide-open bay on the lake; the sun still glitters although evening has arrived in Kuhmo. It's midsummer; the living room has its instruments and other objects in each of its corners.

Parameters:

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- type of linguistic unit
 - sentence
 - paragraph
 - turn in a conversation
 - Web page

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Syntactic context

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Context term is linked to target by a syntactic dependency (e.g. subject, modifier, ...).

The silhouette of the sun beyond a wide-open bay on the lake; the sun still glitters although evening has arrived in Kuhmo. It's midsummer; the living room has its instruments and other objects in each of its corners.

Parameters:

- types of syntactic dependency (Padó and Lapata 2007)
- direct vs. indirect dependency paths
 - direct dependencies
 - direct + indirect dependencies
- homogeneous data (e.g. only verb-object) vs. heterogeneous data (e.g. all children and parents of the verb)
- maximal length of dependency path

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"Knowledge pattern" context

Context term is linked to target by a lexico-syntactic pattern (text mining, cf. Hearst 1992, Pantel & Pennacchiotti 2008, etc.).

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In Provence, Van Gogh painted with bright colors such as red and yellow. These colors produce incredible effects on anybody looking at his paintings.

Parameters:

- inventory of lexical patterns
 - Iots of research to identify semantically interesting patterns (cf. Almuhareb & Poesio 2004, Veale & Hao 2008, etc.)
- ► fixed vs. flexible patterns
 - patterns are mined from large corpora and automatically generalised (optional elements, POS tags or semantic classes)

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In unstructered models, context specification acts as a filter
 determines whether context token counts as co-occurrence
 e.g. muste be linked by any syntactic dependency relation

• e.g. left vs. right context, type of syntactic relation, etc.

In structured models, feature terms are subtyped

depending on their position in the context

Structured vs. unstructured context

Structured vs. unstructured surface context

A dog bites a man. The man's dog bites a dog. A dog bites a man.

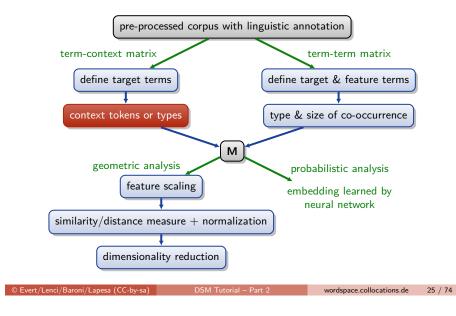
unstructured	bite
dog	4
man	3

A dog bites a man. The man's dog bites a dog. A dog bites a man.

structured	bite-l	bite-r
dog	3	1
man	1	2

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Structured vs. unstructured dependency context		Comparison					
A dog bites a man. The man's dog bites a dog. A dog bites a n unstructured bite dog 4 man 2	nan.	 Unstructured context data less sparse (e.g. man kills and kills man both map to the kill dimension of the vector x_{man}) Structured context 					
A dog bites a man. The man's dog bites a dog. A dog bites a n structured bite-subj bite-obj dog 3 1 man 0 2	nan.	(<i>kill-subj</i> and <i>i</i> ► dependency re the DSM dime "recipient" dim	to semantic distinctions kill-obj are rather differen lations provide a form of ensions (the "subject" di nensions, etc.) account for word-order an	nt things!) f syntactic "typing" of mensions, the			

Overview of DSM parameters

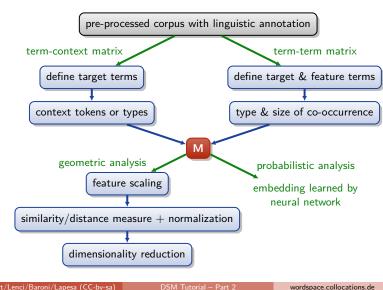


Context tokens vs. context types

- ▶ Features are usually context tokens, i.e. individual instances
 - document, Wikipedia article, Web page, ...
 - paragraph, sentence, tweet,
 - "co-occurrence" count = frequency of term in context token
- Can also be generalised to context types, e.g.
 - type = cluster of near-duplicate documents
 - type = syntactic structure of sentence (ignoring content)
 - type = tweets from same author
 - frequency counts from all instances of type are aggregated
- Context types may be anchored at individual tokens
 - n-gram of words (or POS tags) around target
 - subcategorisation pattern of target verb
 - overlaps with (generalisation of) syntactic co-occurrence

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Marginal and expected frequencies

Matrix of observed co-occurrence frequencies not sufficient

target	feature	0	R	С	Е
dog	small	855	33,338	490,580	134.34
dog	domesticated	29	33,338	918	0.25

Notation

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- O =observed co-occurrence frequency
- \triangleright R = overall frequency of target term = row marginal frequency
- C =overall frequency of feature = column marginal frequency
- N = sample size \approx size of corpus
- Expected co-occurrence frequency

$$E = \frac{R \cdot C}{N} \quad \longleftrightarrow \quad O$$

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Obtaining marginal frequencies

- Term-document matrix
 - \blacktriangleright R = frequency of target term in corpus
 - C = size of document (# tokens)
 - ► *N* = corpus size
- Syntactic co-occurrence
 - # of dependency instances in which target/feature participates
 - ► *N* = total number of dependency instances
 - ► can be computed from full co-occurrence matrix M
- Textual co-occurrence

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- R, C, O are "document" frequencies, i.e. number of context units in which target, feature or combination occurs
- N = total # of context units

Obtaining marginal frequencies

- Surface co-occurrence
 - it is quite tricky to obtain fully consistent counts (Evert 2008)
 - at least correct E for span size k (= number of tokens in span)

$$E = k \cdot \frac{R \cdot C}{N}$$

with R, C = individual corpus frequencies and N = corpus size

- can also be implemented by pre-multiplying $R' = k \cdot R$
- alternatively, compute marginals and sample size by summing over full co-occurrence matrix ($\rightarrow E$ as above, but inflated N)
- NB: shifted PPMI (Levy and Goldberg 2014) corresponds to a post-hoc application of the span size adjustment
 - performs worse than PPMI, but paper suggests they already approximate correct *E* by summing over co-occurrence matrix

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Marginal frequencies in wordspace

DSM objects in wordspace include marginal frequencies as well as counts of nonzero cells for rows and columns.

>	TT\$row	S	
	term	f	nnzero
1	cat	22007	5
2	dog	50807	7
3	animal	77053	7
4	time	1156693	7
5	reason	95047	6
6	cause	54739	5
7	effect	133102	6
>	TT\$col	S	
>	TT\$glo	bals\$N	
[1] 19990	2178	
>	TT\$M #	≠ the full	ςο-οςςι
1	11ψΠ 7	- the full	

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Geometric vs. probabilistic interpretation

► Geometric interpretation

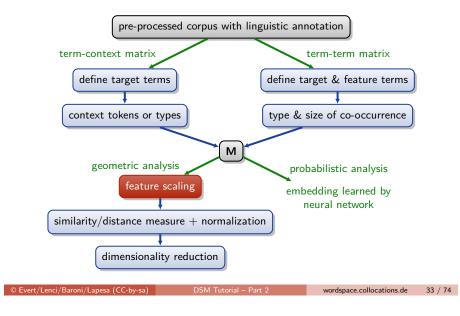
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- row vectors as points or arrows in *n*-dimensional space
- very intuitive, good for visualisation
- use techniques from geometry and matrix algebra
- Probabilistic interpretation
 - co-occurrence matrix as observed sample statistic that is "explained" by a generative probabilistic model
 - e.g. probabilistic LSA (Hoffmann 1999), Latent Semantic Clustering (Rooth *et al.* 1999), Latent Dirichlet Allocation (Blei *et al.* 2003), etc.
 - explicitly accounts for random variation of frequency counts
 - recent work: neural word embeddings

so focus on geometric interpretation in this tutorial

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Feature scaling

Feature scaling is used to "discount" less important features:

- Logarithmic scaling: O' = log(O + 1) (cf. Weber-Fechner law for human perception)
- Relevance weighting, e.g. tf.idf (information retrieval)

$$tf.idf = tf \cdot log(D/df)$$

- ► *tf* = co-occurrence frequency *O*
- df = document frequency of feature (or nonzero count)
- ► *D* = total number of documents (or row count of **M**)
- Statistical association measures (Evert 2004, 2008) take frequency of target term and feature into account
 - often based on comparison of observed and expected co-occurrence frequency

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measures differ in how they balance O and E

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Simple association measures

pointwise Mutual Information (MI)

$$\mathsf{MI} = \log_2 \frac{O}{E}$$

local MI

$$|\text{local-MI} = O \cdot \text{MI} = O \cdot \log_2 \frac{O}{E}$$

t-score

 $t = \frac{O - E}{\sqrt{O}}$

target	feature	0	Ε	MI	local-MI	t-score
dog	small	855	134.34	2.67	2282.88	24.64
dog	domesticated	29	0.25	6.85	198.76	5.34
dog	sgjkj	1	0.00027	11.85	11.85	1.00

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Other association measures

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• simple log-likelihood (\approx local-MI)

$$G^2 = \pm 2 \cdot \left(O \cdot \log_2 \frac{O}{E} - (O - E) \right)$$

with positive sign for O > E and negative sign for O < E

Dice coefficient

$$\mathsf{Dice} = \frac{20}{R+6}$$

~ ~

- Many other simple association measures (AMs) available
- ▶ Further AMs computed from full contingency tables, see
 - Evert (2008)
 - http://www.collocations.de/
 - http://sigil.r-forge.r-project.org/

Applying association scores in wordspace

<pre>> options(digits=3)</pre>	# print fractional values with limited precision
> dsm.score(TT. scor	e="MI", sparse=FALSE, matrix=TRUE)

	breed	tail	feed	kill	important	explain	likely
cat	6.21	4.568	3.129	2.801	-Inf	0.0182	-Inf
dog	7.78	3.081	3.922	2.323	-3.774	-1.1888	-0.4958
animal	3.50	2.132	4.747	2.832	-0.674	-0.4677	-0.0966
time	-1.65	-2.236	-0.729	-1.097	-1.728	-1.2382	0.6392
reason	-2.30	-Inf	-1.982	-0.388	1.472	4.0368	2.8860
cause	-Inf	-0.834	-Inf	-2.177	1.900	2.8329	4.0691
effect	-Inf	-2.116	-2.468	-2.459	0.791	1.6312	0.9221

- ☞ sparseness of the matrix has been lost!
- \bowtie cells with score $x = -\infty$ are inconvenient
- distribution of scores may be even more skewed than co-occurrence frequencies (esp. for local-MI)

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Sparse association scores are cut off at zero, i.e.

$$f(x) = \begin{cases} x & x > 0 \\ 0 & x \le 0 \end{cases}$$

- Also known as "positive" scores
 - ▶ PPMI = positive pointwise MI (e.g. Bullinaria and Levy 2007)
 - wordspace computes sparse AMs by default \rightarrow "MI" = PPMI
- Preserves sparseness if $x \le 0$ for all empty cells (O = 0)
 - sparseness may even increase: cells with x < 0 become empty
- Usually combined with signed association measure satisfying

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- ► x > 0 for O > E
- x < 0 for O < E

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Score transformations

An additional scale transformation can be applied in order to de-skew association scores:

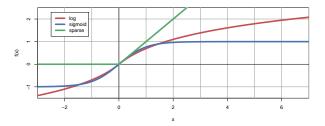
signed logarithmic transformation

$$f(x) = \pm \log(|x|+1)$$

sigmoid transformation as soft binarization

$$f(x) = \tanh x$$

sparse AM as cutoff transformation



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Association scores & transformations in wordspace

<pre>> dsm.score(TT, score="simple-ll", transf="lo # logarithmic co-occurrence frequency</pre>	у							
animal 3.50 2.13 4.75 2.83 0.000 0.0000 0.0 time 0.00 0.00 0.00 0.00 0.000 0.000 0.000 reason 0.00 0.00 0.00 0.00 1.472 4.0368 2.8 cause 0.00 0.00 0.00 0.00 1.900 2.8329 4.0 effect 0.00 0.00 0.00 0.00 0.791 1.6312 0.9 > dsm.score(TT, score="simple-ll", matrix=TRU > dsm.score(TT, score="simple-ll", transf="lo # logarithmic co-occurrence frequency	0							
<pre>time 0.00 0.00 0.00 0.00 0.000 0.000 0.6 reason 0.00 0.00 0.00 0.00 1.472 4.0368 2.8 cause 0.00 0.00 0.00 0.00 1.900 2.8329 4.0 effect 0.00 0.00 0.00 0.00 0.791 1.6312 0.9 > dsm.score(TT, score="simple-ll", matrix=TRU > dsm.score(TT, score="simple-ll", transf="lo # logarithmic co-occurrence frequency</pre>	0							
<pre>reason 0.00 0.00 0.00 0.00 1.472 4.0368 2.8 cause 0.00 0.00 0.00 0.00 1.900 2.8329 4.0 effect 0.00 0.00 0.00 0.00 0.791 1.6312 0.9 > dsm.score(TT, score="simple-ll", matrix=TRU > dsm.score(TT, score="simple-ll", transf="lo # logarithmic co-occurrence frequency</pre>	0							
<pre>cause 0.00 0.00 0.00 0.00 1.900 2.8329 4.0 effect 0.00 0.00 0.00 0.00 0.791 1.6312 0.9 > dsm.score(TT, score="simple-ll", matrix=TRU > dsm.score(TT, score="simple-ll", transf="lo # logarithmic co-occurrence frequency</pre>	9							
<pre>effect 0.00 0.00 0.00 0.00 0.791 1.6312 0.9 > dsm.score(TT, score="simple-ll", matrix=TRU > dsm.score(TT, score="simple-ll", transf="lo # logarithmic co-occurrence frequency</pre>	6							
<pre>> dsm.score(TT, score="simple-ll", matrix=TRU > dsm.score(TT, score="simple-ll", transf="lo # logarithmic co-occurrence frequency</pre>	9							
<pre>> dsm.score(TT, score="simple-ll", transf="lo # logarithmic co-occurrence frequency</pre>	2							
# logarithmic co-occurrence frequency	<pre>> dsm.score(TT, score="simple-ll", matrix=TRUE)</pre>							
	<pre>> dsm.score(TT, score="simple-ll", transf="log", matrix=T)</pre>							
<pre>> dsm.score(TT, score="freq", transform="log"</pre>	# logarithmic co-occurrence frequency							
	<pre>> dsm.score(TT, score="freq", transform="log", matrix=T)</pre>							
# now try other parameter combinations								

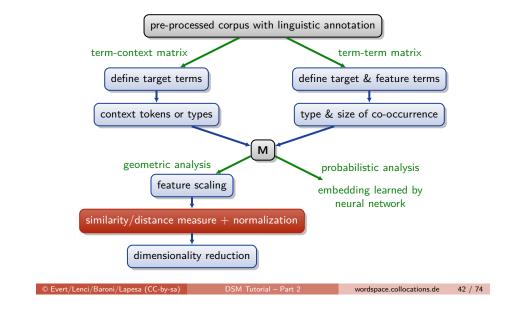
Scaling of column vectors

In statistical analysis and machine learning, features are usually centred and scaled so that

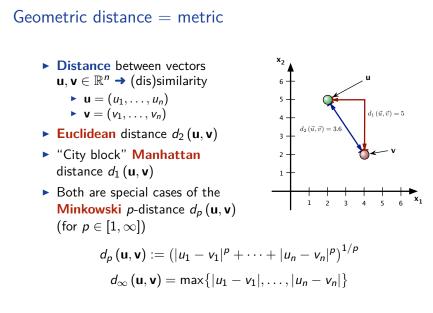
$$\begin{array}{ll} {\rm mean} & \mu = {\rm 0} \\ {\rm variance} & \sigma^2 = {\rm 1} \end{array}$$

- ► In DSM research, this step is less common for columns of M
 - centring is a prerequisite for certain dimensionality reduction and data analysis techniques (esp. PCA)
 - but co-occurrence matrix no longer sparse!
 - scaling may give too much weight to rare features
- M cannot be row-normalised and column-scaled at the same time (result depends on ordering of the two steps)

Overview of DSM parameters



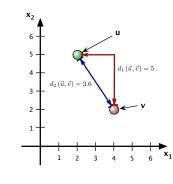
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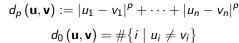


DSM parameters A taxonomy of DSM parameters Geometric distance = metric

$$\mathbf{u}, \mathbf{v} \in \mathbb{R}^n \Rightarrow (dis)$$
similarity

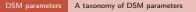
- $\bullet \mathbf{u} = (u_1, \dots, u_n)$ $\bullet \mathbf{v} = (v_1, \dots, v_n)$
- Euclidean distance $d_2(\mathbf{u}, \mathbf{v})$
- "City block" Manhattan distance d₁ (u, v)
- Extension of *p*-distance $d_p(\mathbf{u}, \mathbf{v})$ (for $0 \le p \le 1$)



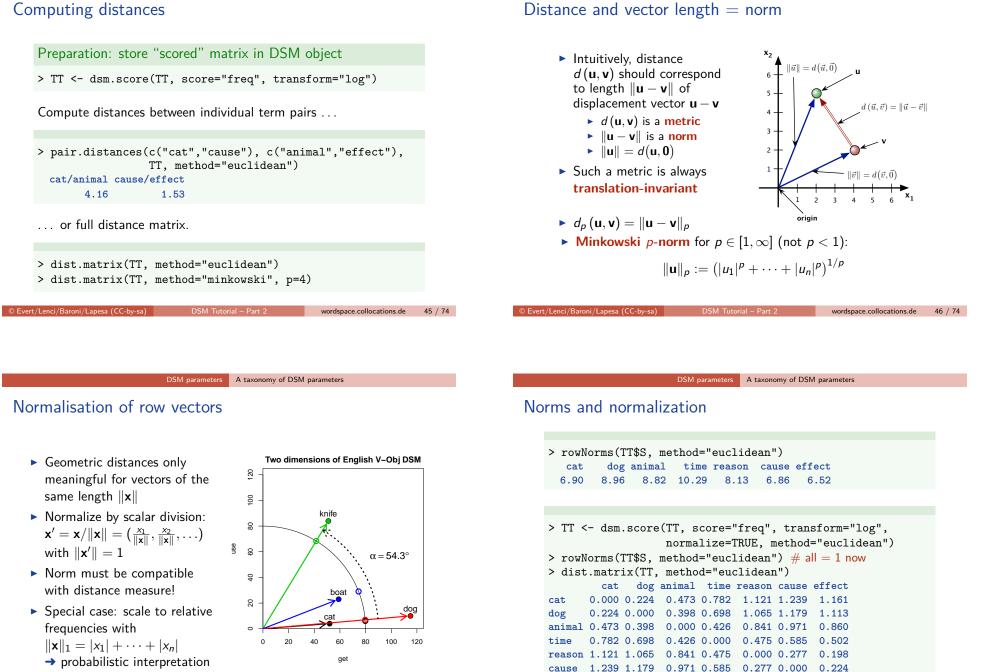


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Computing distances



effect 1.161 1.113 0.860 0.502 0.198 0.224 0.000

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Other distance measures

Information theory: Kullback-Leibler (KL) divergence for probability vectors (☞ non-negative, ||x||₁ = 1)

$$D(\mathbf{u} \| \mathbf{v}) = \sum_{i=1}^{n} u_i \cdot \log_2 \frac{u_i}{v_i}$$

- Properties of KL divergence
 - most appropriate in a probabilistic interpretation of M
 - \blacktriangleright zeroes in ${\bf v}$ without corresponding zeroes in ${\bf u}$ are problematic
 - not symmetric, unlike geometric distance measures
 - ▶ alternatives: skew divergence, Jensen-Shannon divergence
- A symmetric distance measure (Endres and Schindelin 2003)

$$D_{uv} = D(u||z) + D(v||z)$$
 with $z = \frac{u+v}{2}$

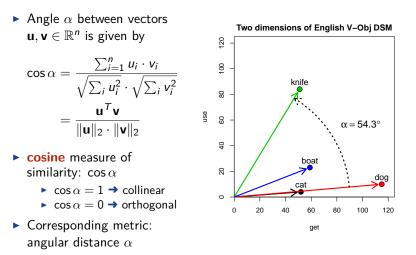
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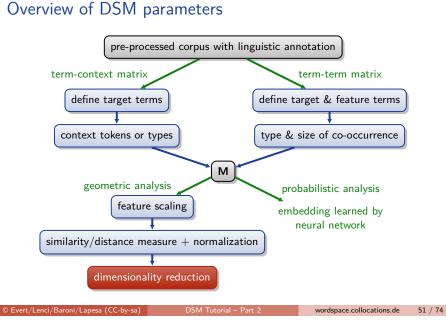
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DSM parameters A taxonomy of DSM parameters

DSM parameters A taxonomy of DSM parameters



Dimensionality reduction = model compression

- Co-occurrence matrix M is often unmanageably large and can be extremely sparse
 - Google Web1T5: 1M × 1M matrix with one trillion cells, of which less than 0.05% contain nonzero counts (Evert 2010)
- Compress matrix by reducing dimensionality (= rows)
- **Feature selection**: columns with high frequency & variance
 - measured by entropy, chi-squared test, nonzero count, ...
 - may select similar dimensions and discard valuable information
 - joint selection of multiple features is useful but expensive
- Projection into (linear) subspace
 - principal component analysis (PCA)
 - independent component analysis (ICA)
 - random indexing (RI)

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intuition: preserve distances between data points

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Dimensionality reduction & latent dimensions

Landauer and Dumais (1997) claim that LSA dimensionality reduction (and related PCA technique) uncovers **latent dimensions** by exploiting correlations between features.

- Example: term-term matrix
- V-Obj cooc's extracted from BNC
 - targets = noun lemmas
 - features = verb lemmas
- feature scaling: association scores (modified log Dice coefficient)
- k = 111 nouns with f ≥ 20 (must have non-zero row vectors)
- n = 2 dimensions: *buy* and *sell*

```
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```

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buv

0.28

-0.52

0.51

-0.01

1.13

-1.05

-0.35

-0.08

1.92

-1.63

noun

bond

dress

land

per

pub

share

system

cigarette

freehold

number

sell

0.77

0.44

-1.30

-0.08

1.54

-1.02

-0.16

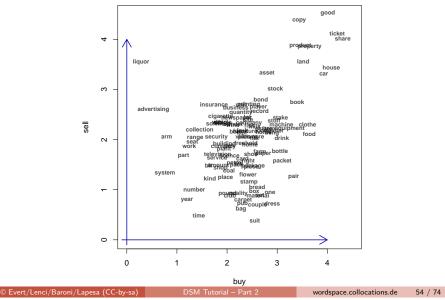
-1.30

1.99

-0.70

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Dimensionality reduction & latent dimensions



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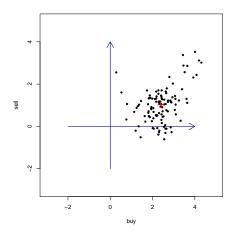
Motivating latent dimensions & subspace projection

- The latent property of being a commodity is "expressed" through associations with several verbs: sell, buy, acquire, ...
- Consequence: these DSM dimensions will be correlated
- Identify latent dimension by looking for strong correlations (or weaker correlations between large sets of features)
- Projection into subspace V of k < n latent dimensions as a "noise reduction" technique → LSA
- Assumptions of this approach:
 - "latent" distances in V are semantically meaningful
 - other "residual" dimensions represent chance co-occurrence patterns, often particular to the corpus underlying the DSM

DSM parameters A taxonomy of DSM parameters

Centering the data set

- Uncentered data set
- Centered data set
- Variance of centered data



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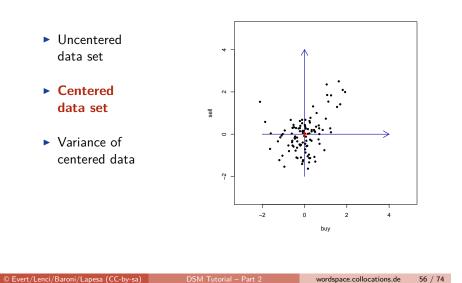
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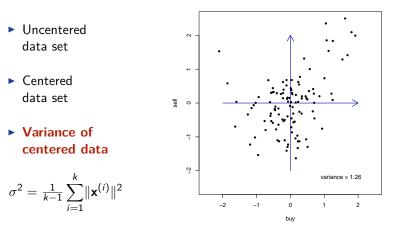
Centering the data set

Centering the data set

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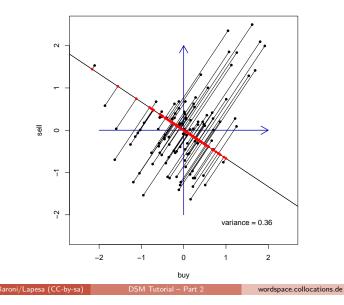
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DSM parameters A taxonomy of DSM parameters

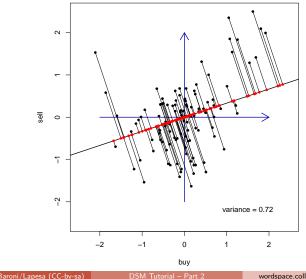
Projection and preserved variance: examples



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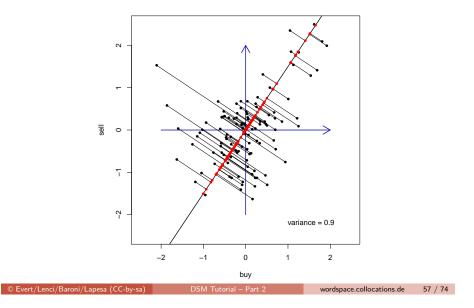
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Projection and preserved variance: examples

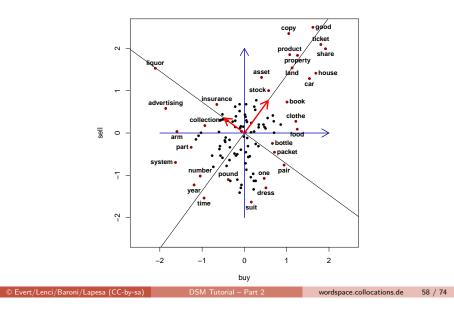


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Projection and preserved variance: examples



Orthogonal PCA dimensions



DSM parameters Examples

DSM parameters A taxonomy of DSM parameters

Dimensionality reduction in practice

```
\# it is customary to omit the centring: SVD dimensionality reduction
> TT2 <- dsm.projection(TT, n=2, method="svd")</pre>
> TT2
                svd2
         svd1
       -0.733 -0.6615
cat
       -0.782 -0.6110
dog
animal -0.914 -0.3606
       -0.993 0.0302
time
reason -0.889 0.4339
cause -0.817 0.5615
effect -0.871 0.4794
> x <- TT2[, 1] # first latent dimension
> y <- TT2[, 2] # second latent dimension
> plot(TT2, pch=20, col="red",
        xlim=extendrange(x), ylim=extendrange(y))
> text(TT2, rownames(TT2), pos=3)
```

Outline

DSM parameters

A taxonomy of DSM parameters Examples

Example: a verb-object DSM

Some well-known DSM examples

Latent Semantic Analysis (Landauer and Dumais 1997)

- term-context matrix with document context
- weighting: log term frequency and term entropy
- distance measure: cosine
- dimensionality reduction: SVD

Hyperspace Analogue to Language (Lund and Burgess 1996)

- term-term matrix with surface context
- structured (left/right) and distance-weighted frequency counts
- distance measure: Minkowski metric $(1 \le p \le 2)$
- dimensionality reduction: feature selection (high variance)

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DSM parameters Examples

Some well-known DSM examples

Infomap NLP (Widdows 2004)

- term-term matrix with unstructured surface context
- weighting: none
- distance measure: cosine
- dimensionality reduction: SVD

Random Indexing (Karlgren and Sahlgren 2001)

- term-term matrix with unstructured surface context
- weighting: various methods
- distance measure: various methods
- dimensionality reduction: random indexing (RI)

DSM parameters Examples

Some well-known DSM examples

Dependency Vectors (Padó and Lapata 2007)

- term-term matrix with unstructured dependency context
- weighting: log-likelihood ratio
- distance measure: PPMI-weighted Dice (Lin 1998)
- dimensionality reduction: none

Distributional Memory (Baroni and Lenci 2010)

- term-term matrix with structured and unstructered dependencies + knowledge patterns
- weighting: local-MI on type frequencies of link patterns
- distance measure: cosine
- dimensionality reduction: none

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Building a DSM Sparse matrices

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A taxonomy of DSM parameters Examples

Building a DSM

Sparse matrices Example: a verb-object DSM

Building a DSM Sparse matrices

Building a DSM Sparse matrices

Scaling up to the real world

- ► So far, we have worked on minuscule toy models
- We want to scale up to real world data sets now
- ► Example 1: window-based DSM on BNC content words
 - ▶ 83,926 lemma types with $f \ge 10$
 - term-term matrix with $83,926 \cdot 83,926 = 7$ billion entries
 - standard representation requires 56 GB of RAM (8-byte floats)
 - only 22.1 million non-zero entries (= 0.32%)
- Example 2: Google Web 1T 5-grams (1 trillion words)
 - more than 1 million word types with $f \ge 2500$
 - term-term matrix with 1 trillion entries requires 8 TB RAM

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• only 400 million non-zero entries (= 0.04%)

<u> </u>	1 State 1 Stat	
Snarco	matrix	representation
Juaise	IIIalin	TEDIESCITALION

Invented example of a sparsely populated DSM matrix

_	eat	get	hear	kill	see	use
boat	.	59	•	•	39	23
cat	.	•	•	26	58	•
cup	.	98	•	•	•	•
dog	33	•	42	•	83	•
knife	.	•	•	•	•	84
pig	9	•	•	27	•	•

Store only non-zero entries in compact sparse matrix format

row	col	value	r	wo	col	value
1	2	59		4	1	33
1	5	39		4	3	42
1	6	23		4	5	83
2	4	26		5	6	84
2	5	58		6	1	9
3	2	98		6	4	27

Building a DSM Example: a verb-object DSM

Building a DSM Sparse matrices

Working with sparse matrices

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- Compressed format: each row index (or column index) stored only once, followed by non-zero entries in this row (or column)
 - convention: column-major matrix (data stored by columns)
- Specialised algorithms for sparse matrix algebra
 - especially matrix multiplication, solving linear systems, etc.
 - take care to avoid operations that create a dense matrix!
- R implementation: Matrix package
 - essential for real-life distributional semantics
 - wordspace provides additional support for sparse matrices (vector distances, sparse SVD, ...)
- Other software: Matlab, Octave, Python + SciPy

Outline

DSM parameters

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A taxonomy of DSM parameters Examples

Building a DSM

Sparse matrices Example: a verb-object DSM

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Triplet tables

- A sparse DSM matrix can be represented as a table of triplets (target, feature, co-occurrence frequency)
 - for syntactic co-occurrence and term-document matrices, marginals can be computed from a complete triplet table
 - > for surface and textual co-occurrence, marginals have to be provided in separate files (see ?read.dsm.triplet)

noun	rel	verb	f	mode
dog	subj	bite	3	spoken
dog	subj	bite	12	written
dog	obj	bite	4	written
dog	obj	stroke	3	written

- DSM_VerbNounTriples_BNC contains additional information
 - syntactic relation between noun and verb
 - written or spoken part of the British National Corpus

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 Additional information can be used for filtering (verb-object relation), or aggregate frequencies (spoken + written BNC)

> tri <- subset(DSM_VerbNounTriples_BNC, rel == "obj")</pre>

Construct DSM object from triplet input

Constructing a DSM from a triplet table

- raw.freq=TRUE indicates raw co-occurrence frequencies (rather than a pre-weighted DSM)
- constructor aggregates counts from duplicate entries
- marginal frequencies are automatically computed
- > VObj # inspect marginal frequencies (e.g. head(VObj\$rows, 20))

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Building a DSM Example: a verb-object DSM

Exploring the DSM

> VObj <-	dsm.sco	re(VObj,	score="N	II", norm	alize=TRUE)
> nearest	0	5	. 0			
horse	cat	animal	rabbit	fish	guy	
73.9	75.9	76.2	77.0	77.2	78.5	
cichlid	kid	bee c	reature			
78.6	79.0	79.1	79.5			
> nearest	.neighbo	urs(VObj	, "dog",	method="	manhattan")
# NB: we u	0	0				
,,						
> VObi50	- dem n	rojectio	n(VObir	n=50 mot	hod="svd")	
-	-		-		nou- svu)	
> nearest	.neighbo	urs(VObj	50, "dog'	')		

uilding a DSM Example: a verb-object DSM

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References I

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- Baroni, Marco and Lenci, Alessandro (2010). Distributional Memory: A general framework for corpus-based semantics. *Computational Linguistics*, 36(4), 673–712.
- Blei, David M.; Ng, Andrew Y.; Jordan, Michael, I. (2003). Latent Dirichlet allocation. *Journal of Machine Learning Research*, **3**, 993–1022.
- Bullinaria, John A. and Levy, Joseph P. (2007). Extracting semantic representations from word co-occurrence statistics: A computational study. *Behavior Research Methods*, **39**(3), 510–526.
- Endres, Dominik M. and Schindelin, Johannes E. (2003). A new metric for probability distributions. *IEEE Transactions on Information Theory*, **49**(7), 1858–1860.
- Evert, Stefan (2004). The Statistics of Word Cooccurrences: Word Pairs and Collocations. Dissertation, Institut für maschinelle Sprachverarbeitung, University of Stuttgart.
- Evert, Stefan (2008). Corpora and collocations. In A. Lüdeling and M. Kytö (eds.), Corpus Linguistics. An International Handbook, chapter 58, pages 1212–1248. Mouton de Gruyter, Berlin, New York.
- Evert, Stefan (2010). Google Web 1T5 n-grams made easy (but not for the computer). In *Proceedings of the 6th Web as Corpus Workshop (WAC-6)*, pages 32–40, Los Angeles, CA.

Building a DSM Example: a verb-object DSM

References II

- Hoffmann, Thomas (1999). Probabilistic latent semantic analysis. In Proceedings of the Fifteenth Conference on Uncertainty in Artificial Intelligence (UAI'99).
- Karlgren, Jussi and Sahlgren, Magnus (2001). From words to understanding. In Y. Uesaka, P. Kanerva, and H. Asoh (eds.), *Foundations of Real-World Intelligence*, chapter 294–308. CSLI Publications, Stanford.
- Landauer, Thomas K. and Dumais, Susan T. (1997). A solution to Plato's problem: The latent semantic analysis theory of acquisition, induction and representation of knowledge. *Psychological Review*, **104**(2), 211–240.
- Levy, Omer and Goldberg, Yoav (2014). Neural word embedding as implicit matrix factorization. In *Proceedings of Advances in Neural Information Processing Systems 27*, pages 2177–2185. Curran Associates, Inc.
- Lin, Dekang (1998). Automatic retrieval and clustering of similar words. In *Proceedings of the 17th International Conference on Computational Linguistics (COLING-ACL 1998)*, pages 768–774, Montreal, Canada.
- Lund, Kevin and Burgess, Curt (1996). Producing high-dimensional semantic spaces from lexical co-occurrence. Behavior Research Methods, Instruments, & Computers, 28(2), 203–208.

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Padó, Sebastian and Lapata, Mirella (2007). Dependency-based construction of semantic space models. *Computational Linguistics*, **33**(2), 161–199.

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References III

- Rooth, Mats; Riezler, Stefan; Prescher, Detlef; Carroll, Glenn; Beil, Franz (1999). Inducing a semantically annotated lexicon via EM-based clustering. In *Proceedings of the 37th Annual Meeting of the Association for Computational Linguistics*, pages 104–111.
- Widdows, Dominic (2004). *Geometry and Meaning*. Number 172 in CSLI Lecture Notes. CSLI Publications, Stanford.